

Tutorial 3

Logic Circuit Design

CO 2206 Computer Organization

Task 1: Karnaugh Map Exercise

- Simplify the following Boolean functions using Karnaugh map:
 - $F(x,y,z) = \sum m(0,1,5,7)$
 - $F(x,y,z) = \sum m(0,1,2,4,6)$
 - $F(w,x,y,z) = \sum m(1,4,6,7,8,9,10,11,15)$
 - $F(A,B,C,D) = \sum m(0,2,5,6,8,10,13,14,15)$
- Find the simplest sum of products form for the function F using the don't care condition G , where
 - $F(a,b,c,d) = \sum m(0,2,8,10,14)$ and
 - $G(a,b,c,d) = \sum m(5,7,12,13)$
- Simplify $F(A,B,C,D) = \prod M(1,3,4,6,9,11)$ together with the don't care conditions $d(A,B,C,D) = \sum m(0,2,5,10,12,14)$ in (i) *sum of products* and (ii) *products of sums*
- Simplify the even parity function using XOR

Task 2: Quine-McCluskey

- Minimize the following functions using the *Quine-McCluskey* minimization:
 - $F(x,y,z) = \sum m(0,1,2,4,6)$
 - $f_1(x_1, x_2, x_3, x_4) = \sum m(0, 6, 7, 9, 13, 14, 15)$
 - $f_2(x_1, x_2, x_3, x_4, x_5) = \sum m(0, 2, 6, 10, 13, 16, 18, 20, 21, 23, 24, 26, 30, 31)$

Task 3: Implementation

- Ignoring gate-input cost:
 - Implement all functions in **Task 1** using any combination of logic gates
 - Implement all functions in **Task 2** using *NAND* only
 - Draw the *NOR* implementation of the function $F = \Sigma m(0,1,2,8,10,11,14,15)$. Hint: Use $F' = \text{SOP}$.